

Function Features

A function f
is concave up if...



Function Features

A function f
is concave down if...



Function Features

A function f
is increasing on an
interval if...



Function Features

A function f
is decreasing on an
interval if...



Function Features

Average rate of change
of f on the interval $[a, b]$



Function Features

The slope of a function
at any given point
gives...



Function Features

A positive rate of change
indicates that the function
output is...



Function Features

A negative rate of change
indicates that the function
output is...



Function Features

Point of inflection



Function Features

One-to-one function



<p>The rates of change of f are decreasing</p>	<p>The rates of change of f are increasing</p>
<p>As the input values increase, the output values always decrease.</p> <p>OR</p> <p>For all a and b in the interval, if $a < b$, then $f(a) > f(b)$.</p>	<p>As the input values increase, the output values always increase.</p> <p>OR</p> <p>For all a and b in the interval, if $a < b$, then $f(a) < f(b)$.</p>
<p>The rate of change of the function at that input</p>	$\frac{f(b) - f(a)}{b - a}$
<p>Decreasing</p>	<p>Increasing</p>
<p>Function where each input has a unique output (no repeated outputs)</p>	<p>Point on the graph of a function where the concavity changes, indicating a maximum or minimum rate of change</p>

Function Features

A relative minimum occurs when a function f ...



Function Features

A relative maximum occurs when a function f ...



Function Features

Absolute minimum



Function Features

Absolute maximum



Function Features

Multiplicity



Function Features

A polynomial of degree n has...



Function Features

If $x = a$ is a real zero of a polynomial with an odd multiplicity, then...



Function Features

If $x = a$ is a real zero of a polynomial with an even multiplicity, then...



Function Features

Odd function



Function Features

Even function



Changes from increasing to decreasing	Changes from decreasing to increasing
The greatest output of a function	The least output of a function
<ul style="list-style-type: none"> • Exactly n complex zeros (real or imaginary) • Constant nth differences • At most $n - 1$ extrema 	The number of times a factor occurs in a polynomial function
The graph of the polynomial is tangent to the x -axis at $x = a$.	The graph of the polynomial passes through the x -axis at $x = a$.
$f(-x) = f(x)$	$f(-x) = -f(x)$

Function Features

End behavior of a polynomial f with an even degree and a negative leading coefficient



Function Features

End behavior of a polynomial f with an odd degree and a positive leading coefficient



Function Features

End behavior of a polynomial f with an odd degree and a negative leading coefficient



Function Features

End behavior of a polynomial f with an even degree and a positive leading coefficient



Function Features

If a rational function, f , has a horizontal asymptote at $y = b$, then...



Function Features

To determine the end behavior of a rational function...



Function Features

A rational function has a zero at $x = a$ if...



Function Features

A rational function has a hole at $x = a$ if...



Function Features

A rational function has a vertical asymptote at $x = a$ if...



Function Features

For rational functions, a slant asymptote occurs when...



$$\lim_{x \rightarrow \infty} f(x) = \infty$$

$$\lim_{x \rightarrow -\infty} f(x) = -\infty$$

$$\lim_{x \rightarrow \infty} f(x) = -\infty$$

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$$\lim_{x \rightarrow -\infty} f(x) = \infty$$

$$\lim_{x \rightarrow \infty} f(x) = -\infty$$

$$\lim_{x \rightarrow -\infty} f(x) = \infty$$

Analyze the ratio of leading terms

The ratio of leading terms is a constant, b ,
 $\lim_{x \rightarrow \infty} f(x) = b$, and
 $\lim_{x \rightarrow -\infty} f(x) = b$

$x = a$ is a zero of the numerator AND the denominator

$x = a$ is a zero of the numerator but NOT the denominator

The degree of the numerator is exactly one more than the degree of the denominator

$x = a$ is a zero of the denominator but NOT the numerator

Function Features

If a rational function, f , has a vertical asymptote at $x = a$, then $\lim_{x \rightarrow a^-} f(x) = \underline{\hspace{2cm}}$ and $\lim_{x \rightarrow a^+} f(x) = \underline{\hspace{2cm}}$.



Function Features

If a rational function, f , has a hole at (a, L) then $\lim_{x \rightarrow a^-} f(x) = \lim_{x \rightarrow a^+} f(x) = \underline{\hspace{2cm}}$.



Function Features

A function $f(x) = ab^x$ demonstrates exponential growth if...



Function Features

A function $f(x) = ab^x$ demonstrates exponential decay if...



Function Features

Key features of $y = \log_b x$ where $b > 1$



Function Features

Key features of $y = b^x$ where $b > 1$



Properties and Identities

$$b^{x+c} =$$



Properties and Identities

$$b^{x-c} =$$



Properties and Identities

$$e^{a \ln b} =$$



Properties and Identities

$$\log_b(1) =$$



L	$\pm\infty ; \pm\infty$
$0 < b < 1$	$b > 1$
<ul style="list-style-type: none"> • Domain: all real numbers • Range: $y > 0$ • Horizontal asymptote at $y = 0$ • Increasing and concave up over entire domain 	<ul style="list-style-type: none"> • Domain: $x > 0$ • Range: all real numbers • Vertical asymptote at $x = 0$ • Increasing and concave down over entire domain
$\frac{b^x}{b^c}$	$b^x \cdot b^c$
0	b^a

Properties and Identities

$$\log_b(b) =$$



Properties and Identities

$$\log_b(mn)$$



Properties and Identities

$$\log_b\left(\frac{m}{n}\right)$$



Properties and Identities

$$\log_b m^k$$



Properties and Identities

Pythagorean
Identities



Properties and Identities

$$\begin{aligned}\sec \theta &= \\ \csc \theta &= \\ \cot \theta &= \end{aligned}$$



Properties and Identities

$$\cos(\alpha \pm \theta)$$



Properties and Identities

$$\sin(\alpha \pm \theta)$$



Properties and Identities

$$\cos(2\theta)$$



Properties and Identities

$$\sin(2\theta)$$



$\log_b m + \log_b n$	1
$k \log_b m$	$\log_b m - \log_b n$
$\frac{1}{\cos \theta}$ $\frac{1}{\sin \theta}$ $\frac{1}{\tan \theta} = \frac{\cos \theta}{\sin \theta}$	$\sin^2 \theta + \cos^2 \theta = 1$ $1 + \cot^2 \theta = \csc^2 \theta$ $\tan^2 \theta + 1 = \sec^2 \theta$
$\sin \alpha \cos \theta \pm \sin \theta \cos \alpha$	$\cos \alpha \cos \theta \mp \sin \alpha \sin \theta$
$2 \sin \theta \cos \theta$	$\cos^2 \theta - \sin^2 \theta$ $= 2 \cos^2 \theta - 1$ $= 1 - 2 \sin^2 \theta$

Polar Functions

Given (x, y) in Cartesian coordinates, determine polar coordinates, (r, θ)



Polar Functions

Given (r, θ) in polar coordinates, determine Cartesian coordinates, (x, y)



Polar Functions

A polar function $r = f(\theta)$ is increasing if...



Polar Functions

A polar function $r = f(\theta)$ is decreasing if...



Polar functions

The distance between a point on a polar function $r = f(\theta)$ and the origin is increasing if...



Polar functions

The distance between a point on a polar function $r = f(\theta)$ and the origin is decreasing if...



Describing Growth in Functions

A function is linear if over equal-length input intervals, output values _____.



Describing Growth in Functions

A function is quadratic if over equal-length input intervals, output values _____.



Describing Growth in Functions

A function is exponential if as input values change _____, output values change _____.



Describing Growth in Functions

A function is logarithmic if as input values change _____, output values change _____.



$x = r \cos \theta$ $y = r \sin \theta$	$r = \sqrt{x^2 + y^2}$ $\theta = \tan^{-1} \left(\frac{y}{x} \right)$ <p>(*Add π if angle is in Q2 or Q3)</p>
<p>As θ increases, r decreases.</p>	<p>As θ increases, r increases.</p>
<p>r is positive and decreasing or r is negative and increasing. (r is decreasing)</p>	<p>r is positive and increasing or r is negative and decreasing. (r is increasing)</p>
<p>Change by a constant second difference.</p>	<p>Change by a constant amount.</p>
<p>multiplicatively; additively</p>	<p>additively; multiplicatively</p>

Describing Growth in Functions

The average rates of change of a linear function are...



Describing Growth in Functions

The average rates of change of a quadratic function...



Trig Functions

$\tan \theta$ gives the _____ of the terminal ray of θ .



Trig Functions

Domain and range of $y = \arcsin x$



Trig Functions

Domain and range of $y = \arccos x$



Trig Functions

Domain and range of $y = \arctan x$



Trig Functions

$f(x) = \tan x$ has vertical asymptotes at...



Trig Functions

$f(x) = \cot x$ has vertical asymptotes at ...



Trig Functions

Determine the amplitude, period, midline, and phase shift of $f(x) = a \sin(b(x - c)) + d$



Trig Functions

$y = \tan(bx)$ has a period of...



<p>Are changing at a constant rate OR follow a linear pattern</p>	<p>Constant</p>
<p>Domain: $[-1,1]$ Range: $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$</p>	<p>Slope</p>
<p>Domain: $(-\infty, \infty)$ Range: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$</p>	<p>Domain: $[-1,1]$ Range: $[0, \pi]$</p>
<p>$x = \pi k$, where k is an integer</p>	<p>$x = \frac{\pi}{2} + \pi k$, where k is an integer</p>
<p>$\frac{\pi}{b}$</p>	<p>Amplitude = a Period = $\frac{2\pi}{b}$ Midline: $y = d$ Phase shift: c units to the right</p>

Trig Functions

Key features of
 $y = \sin x$



Trig Functions

Key features of
 $y = \cos x$



Transformations

$$f(x) + c$$



Transformations

$$f(x - c)$$



Transformations

$$cf(x)$$



Transformations

$$f(cx)$$



Transformations

$$-f(x)$$



Transformations

$$f(-x)$$



Miscellaneous

Pascal's Triangle



Miscellaneous

What does
the constant e
represent?



<ul style="list-style-type: none"> • Domain: all real numbers • Range: $[-1, 1]$ • Period: 2π • Amplitude: 1 • Midline: $y = 0$ • Passes through $(0, 1)$ 	<ul style="list-style-type: none"> • Domain: all real numbers • Range: $[-1, 1]$ • Period: 2π • Amplitude: 1 • Midline: $y = 0$ • Passes through $(0, 0)$
<p>Horizontal translation c units to the right if $c > 0$ or c units to the left if $c < 0$</p>	<p>Vertical translation c units up if $c > 0$ or c units down if $c < 0$</p>
<p>Horizontal dilation by a factor of $\frac{1}{c}$</p>	<p>Vertical dilation by a factor of c</p>
<p>Reflection over the y-axis</p>	<p>Reflection over the x-axis</p>
<p>The base rate of growth for all continually growing processes $e \approx 2.718$</p>	<p style="text-align: center;"> 1 1 1 1 2 1 1 3 3 1 1 4 6 4 1 1 5 10 10 5 1 1 6 15 20 15 6 1 1 7 21 35 35 21 7 1 </p>

Miscellaneous

A positive residual indicates that the predicted value is an

_____.



Miscellaneous

A negative residual indicates that the predicted value is an

_____.



Miscellaneous

Explicit rule for n th term of a geometric sequence given common ratio r , and the a_k term



Miscellaneous

Explicit rule for n th term of an arithmetic sequence given common difference d , and the a_k term



Miscellaneous

Residual



Miscellaneous

A model is considered appropriate for a data set if the residual plot...



Miscellaneous

Error (in a model)



Miscellaneous

f and g are inverse functions if...



Miscellaneous

If the y -axis is logarithmically scaled, then...



Miscellaneous

In a semi-log plot where the y -axis is logarithmically scaled, exponential functions will appear



Overestimate	Underestimate
$a_n = a_k + d(n - k)$	$a_n = a_k \cdot r^{n-k}$
Appears without pattern	Actual value - Predicted value
$f(g(x)) = g(f(x)) = x$	Predicted value - Actual value
linear	Equal-sized increments on the y-axis represent proportional changes in the output variable