# AP Statistics CED 9.1 Daily Video 1 (Skill 1.A) Introducing Statistics – Do Those Points Align?

Introducing Statistics – Do Those Points Align?		
What Will We Learn?		
How can we determine if the slope of a sample regression line is consistent with random variation		
from a population regression model?		
How Faithful is Old Faithful?		
The Old Faithful geyser is the most popular attraction in Yellowstone National Park. People travel		
from all over the world to see this geyser erupt. The National Park Service helps visitors plan their		
time in the park by when Old Faithful will erupt next. The Starnes family took its first trip to		
Yellowstone National Park in July 1995. They only had six hours in the park, but were able to see Old		
Faithful erupt. Mr. and Mrs. Starnes returned to the park in July 2019. They wondered if the model		
used to predict eruptions of Old Faithful was still the same as in 1995.		
Old Faithful: 1995		
This scatterplot displays data on the duration (in minutes) and wait time until the next eruption (in		
minutes) for all 262 recorded eruptions of Old Faithful in July 1995. predicted wait time = 33.34 + 13.29(duration)		
There is a,,,		
and		
in this population of Old Faithful eruptions.		
Its equation is:		
predicted wait time = 33.34 + 13.29 (duration)		
Old Faithful: 2019		
The scatterplot displays data on the duration (in minutes) and wait time until the next eruption (in		
minutes) for a random sample of 25 Old Faithful eruptions in July 2019.		
There is a,,,		
relationship between and		
in this population of Old Faithful eruptions.		
Its equation is		
predicted wait time = 62.95 + 7.79 (duration)		
Old Faithful: Then and Now		
Is it believable that the population regression model from 1995 is still valid for predicting wait time		
from the duration of the previous Old Faithful eruption in 2019? July 1995 Population (N = 262)		
predicted wait time = 33.34 + 13.29(duration)		
We need to the of getting a		
sample regression line with a as least as unusual as		
7.79 in a random sample of $n = 25$ observations from the July 1995		
population.		
50		
July 2019. Sample ( $n = 25$ ) yielded a:		
predicted wait time = 62.95 + 7.79(duration)		

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regression line with a \_\_\_\_\_ at least as unusual as \_\_\_\_\_ in a random sample of n = 25 observations from the July, 1995 population.

Looking at the sampling distribution, we see that we never got a slope of 7.79, so our estimated probability  $\approx$ \_\_\_\_\_

#### Old Faithful: Simulation Results

Is it believable that the population regression model from 1995 is still valid for predicting wait time from the duration of the previous Old Faithful eruption in 2019?

There is an	0 probability	of obtaining a	regression
line with a	_ as least as surprising (in	directions) as 7.79 is th	e population
regression model from	is still		
What Should We Take Away?			
<ul> <li>Take random samples of size from the population.</li> </ul>			
Calculate the	of each sample regression l	ine.	

- Build the \_\_\_\_\_ distribution of the slope.
- See if the \_\_\_\_\_\_ value of the sample slope can be explained by \_\_\_\_\_\_ variation or not.



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13

Slope of Sample Regression Line

14

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## AP Statistics CED 9.2 Daily Video 1 (Skill 1.D)

Confidence Intervals for the Slope of a Regression Model

1 5	
What Will We Learn?	
Nhat conditions must the population regression model meet to obtain v	valid confidence intervals and
significance tests for the slope?	
How can we determine the shape, center and variability of the sampling	distribution of the slope of a
sample regression line?	
s Old Faithful Still Faithful?	
The Starnes family took its first trip to Yellowstone National Park in July <sup>•</sup>	1995. They only had six hours
n the park, but were able to see Old Faithful erupt. Mr. and Mrs. Starne	s returned to the park in July
2019. They wondered if the model used to predict eruptions of Old Fait	hful was still the same as in
1995. Earlier, we used simulation to determine that the answer is "No."	
Can we construct a confidence interval for the slope of the population re	egression line in 2019? To
answer that question, we need to understand the connection between t	he population regression
nodel and the sampling distribution of the slope.	
Old Faithful: 1995	predicted wait time = $33.34 + 13.29$ (duration)
The scatterplot displays data on the duration (in minutes) and wait	110-
ime until the next eruption (in minutes) for all 262 recorded eruptions	
of Old Faithful in July, 1995. We have added the population	08 00 00 00 00 00 00 00 00 00 00 00 00 0
line to scatterplot. Its equation is:	
	)) 50 <b>1</b>
predicted wait time = 33.34 + 13.29(duration)	1.5 2 2.5 3 3.5 4 4.5 5 Duration (min)
Old Faithful: 2019	
The scatterplot displays data on the duration (in minutes) and wait time	until the next eruption (in
ninutes) for a random sample of 25 Old Faithful eruptions in July 2019.	predicted wait time = 62.95 + 7.79(duration)
	102- • • • 100- • • •
Ne have added the line to the	(ijiu) yu
scatterplot. Its equation is:	11 He M 92-
	90 ) 88-
predicted wait time = $62.95 + 7.79$ (duration)	35 36 37 38 39 4 41 42 43 44 45 Derxtina (min) © Daren Stames
Can we construct a confidence interval for the slope of the population re	earession line in 2019?
	5
Simulated Sampling Distribution	predicted wait time = 33.34 + 13.29(duration)
Suppose we take random sample of $n = 25$	•••
observations from the of eruptions in July,	
1995 and calculate the sample regression line $\hat{y} = a + bx$ for each $\hat{y} = a + bx$	
one.	
70	30 BP 332 00
Can we determine the shape, center and variability of the	
50	1 1 <b>3</b> 8

sampling distribution of the slope b of the sample regression line from the population regression model?



3 3.5 Duration (min) 4.5

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1.5 2 2.5

Nar	ne
Simulated Sampling Distribution	
Suppose we take repeated random samples of $n = 25$	July 1995 Population ( $N = 262$ )
observations from the population of eruptions in July 1995 and	predicted wait time = $33.34 + 13.29$ (duration)
calculate the sample regression line $\hat{v} = a + bx$ for each one.	Simulated sampling distribution of the slope of
Can we determine the shape, center and variability of the	of size $n = 25$ from the July 1995 population
sampling distribution of the slope $h$ of the sample regression	
line from the population model?	
What are the shape, center and variability of the simulated	
sampling distribution of the slope of the sample regression line	
$\hat{y} = a \pm hr^2$	10 11 12 13 14 15 16 17
y = u + bx:	Slope of Sample Regression Line © Daren Starnes
<b>Sampling Distribution of</b> <i>b</i> (Use the distribution above.)	
Shape: How are these ch	naracteristics related to the
Center: population regre	ssion model?
Variability:	
Population Regression Model	
The population regression model is $\mu_y = \alpha + \beta x$ where $\mu_y$ is	
the mean value of the variable <i>y</i> for a	
given value of the variable <i>x</i> .	$\mu_{\mathbf{y}} = \alpha + \beta \mathbf{x}$
	×
Confidence intervals and significance test for the slope $eta$	© Daren Starnes
require that the population regression model meet these	
conditions:	
The relationship between x and y is	·
• The standard deviation of $y, \sigma_y$ does not with	۱ <i>x</i> .
For a particular value of <i>x</i> , the responses () ar	e approximately normally distributed.
Population Regression Model	
Confidence intervals and significance test for the slope $eta$ require	e that the population regression
model meet these conditions:	
• The true relationship between x and y is linear. To check	c this:
Scatterplot: The scatterplot shows a	
relationship between duration and wait time.	
Residual Plot: The residual plot show scatt	er about Residual = line and no
evidence of a curved pattern.	
• The standard deviation of $y, \sigma_y$ , does not vary with $x$ .	
Scatterplot: The wait times by a	amount for the different eruption
durations in the data set.	
Residual Plot: The residuals are in for t	he eruption durations in the data set.
	·
• For a particular value of x, the responses () ar	e approximately normally distributed.
Dotplot: A dotplot of residuals is roughly	,, and
somewhat	
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Sampling Distribution of Slope	
When a population regression model $\mu_y = \alpha + \beta x$ meets the co	nditions, the sampling distribution of
the slope $b$ of the sample regression line has: July 1	995 Population ( <i>N</i> = 262)
Shape:	$n_{e} = 33.34 + 13.29$ (duration)
100 -	
Center: $\mu_b = \beta = $ $\sigma =$	6.47
80-	
Variability: $\sigma_{h} = \frac{\sigma}{m}$	6
$\sigma_x \sqrt{n}$	$\sigma_x = 1.18$
	2.5 3 3.5 4 4.5 5 Duration (min)
where: = Standard deviation of for the popul	ation regression line and
= Standard deviation of in population	and
= sample size.	
Sampling Distribution of Slope	July 1995 Population ( $N$ = 262)
Suppose we take every possible random sample of	$\mu_{\text{wait time}} = 33.34 + 13.29$ (duration) Simulated sampling distribution of the slope of
observations from the population and calculate the sample	the sample regression line based on samples of size $n = 25$ from the July 1995 population
regression line $y = a + bx$ for each one.	
Sampling distribution of <i>b</i>	SD = 1.10
Shape:	
Center: $\mu_b = \beta = $	
	10 11 12 13 14 15 16 17
Variability: $\sigma_b = \frac{\sigma}{\sigma \sqrt{n}} = $	Slope of Sample Regression Line © Daren Starnes
$\sigma_{\chi}$ v $n$	
When sampling without replacement check: (if $n \le 10\%$ N)	
Inference for Slope	
Can we construct a confidence interval for the slope of the popu	Ilation regression line in 2019?
Related guestions:	5
How do we check the conditions about the	regression model using only the
data?	
How can we the standard deviation of the	distribution of the
$\sigma_{\rm c} = \frac{\sigma}{\sigma_{\rm c}}$ when we do not know the values of	
sample slope, $\sigma_b = \frac{\sigma_x \sqrt{n}}{\sigma_x \sqrt{n}}$ , when we do not know the values of	$\sigma$ or $\sigma_x$ :
What Should We Take Away?	
What conditions must the population regression model meet to	obtain valid confidence intervals and
• The relationship between x and y is	·
• The standard deviation of $y, \sigma_y$ , does w	
• For a particular value of x, the responses are	approximately normally distributed.
How can we determine the shape, center and variability of the sa	ampling distribution of the slope of a
sample regression line?	<i>a</i>
Shape: Approximately normal; Center: $\mu_b=~eta$	Variability: $\sigma_b = rac{\sigma}{\sigma_x \sqrt{n}}$



## AP Statistics CED 9.2 Daily Video 2 (Skill 4.C)

Confidence Intervals for the Slope of a Regression Model

#### What Will We Learn?

How do we identify an appropriate confidence interval procedure for the slope of a population regression line?

How do we verify the conditions for calculating a confidence interval for the slope of a population regression line?

#### Predicting Old Faithful in 2019

The Starnes family took its first trip to Yellowstone National Park in July 1995. They only had six hours in the park, but were able to see Old Faithful erupt. Mr. and Mrs. Starnes returned to the park in July 2019. They wondered if the model used to predict eruptions of Old Faithful was still the same as in 1995. Earlier, we used simulation to determine that the answer is "No."

Can we construct a confidence interval for the slope of the population regression line in 2019?

**Old Faithful: 2019** The scatterplot displays data on the duration (in minutes) and wait time until the next eruption (in minutes) for a random sample of 25 Old Faithful eruptions in July 2019, along with the sample regression line. Computer output from a least-squares regression analysis is shown below:



redictor	COGI	SE COGI	I-value	P-value
Constant	62.95	16.4	3.85	0.001
Duration(min)	7.79	4.03	1.94	0.065
5=4.20970	R-sq=1	4.01%	R-sq(ad	ij)=10.27%

Coof CE Coof T-Value

Can we construct a confidence interval for the slope of the population regression line in 2019? **Population Regression Model** 

# The population regression model is $\mu_y = \alpha + \beta x$ where $\mu_y$ is the mean value of the \_\_\_\_\_\_\_ variable y for a given value of the \_\_\_\_\_\_\_ variable x. Confidence intervals and

significance tests for the slope eta require that the population regression model meet three conditions:

- The \_\_\_\_\_ relationship between x and y is \_\_\_\_\_
- The standard deviation of y,  $\sigma_y$  does not \_\_\_\_\_ with x.
- For a particular value of x, the responses (\_\_\_\_\_) are approximately normally distributed.

#### Sampling Distribution of Slope













## AP Statistics CED 9.2 Daily Video 3 (Skill 3.D)

Confidence Intervals for the Slope of a Regression Model

What Will We Learn?		
How do we determine the margin of error when estimating the slope of a population regression line?		
How do we calculate a confidence interval for the slope of a population regression line?		
Predicting Old Faithful: 2019 predicted wait time = 62.95 + 7.79(duration)		
The scatterplot displays data on the duration (in minutes) and wait time		
until the next eruption (in minutes) for a random sample of 25 Old		
Faithful eruptions in July 2019, along with the sample regression line.		
Computer output from a Predictor Coef SE Coef T-Value P-Value		
least-square regression Duration (min) 7.79 4.03 1.94 0.065		
analysis is shown below. S=4.20970 R-sq=14.01% R-sq(adj)=10.27% 35 36 37 38 39 4 41 42 43 44 45		
Calculate and interpret a 95% confidence interval for the slope of the population regression line in		
2019.		
Calculating the Margin of Error		
In AP Statistics, confidence intervals have the form:		
Cl = ±		
The margin of error describes how a value of a statistic is to vary		
from the value of the population		
The margin of error is determined by factors:		
How much the statistic varies from the		
<ul> <li>How we want to be in our</li> </ul>		
margin of error = ()()		
Standard Error of Slope		
The standard error of a statistic is an of the of the sampling		
distribution of the		
From topic 9.2, the standard deviation of the sampling distribution of $b$ is:		
$\sigma_{\rm h} = \frac{\sigma}{1}$		
$\sigma_{b} = \sigma_{x} \sqrt{n}$		
Because we don't know the value of $\sigma$ or $\sigma_x$ , we estimate them using the standard deviation of		
for the sample regression line, <i>s</i> , and the standard deviation of the <i>x</i> -values in the		
sample, <i>s<sub>x</sub></i> , to get the:		
$SE_{r} = \frac{S}{1}$		
$SL_b = S_x \sqrt{n-1}$		
Calculating the Margin of Error		
The critical value is a that makes the margin of error large enough to give a specific		
amount of confidence that the contains the value of the		
From confidence intervals for the of a population regression line, the		
represent the encompassing the middle of the with		
degrees of freedom , where C% is the .		



	Name	
Calculating the Margin of Error		
= (critical value)	)(standard error of statistic)	
In the Old Faithful example, we are asked	to construct a 95% confidence	
interval based on a random sample of $n =$	25 eruptions. To find the	
critical value for a 95% confidence	interval, find the	
encompassing the middle	e of the	
with	This value can be found using $-t^* = -2.069$ $t^* = 2.069$	
Table B or using technology using InvT. Fi	ther way the critical value $t^* =$	
Calculating the Confidence Interval		
C = + (	)/	
$C_{1} = b + t^{*}S_{2} = b + t^{*} = \frac{s}{s}$		
$CI = D \pm t \ SL_b = D \pm t \ \frac{1}{s_x \sqrt{n-1}}$	For our example about Old Faithful eruptions, $b=$	
(Use this space to calculate the CI)	and $s = $ Unfortunately, $s_x$ is not shown in the	
(contrast parts to cantality and ca	computer regression output. From the previous video,	
S		
	Predictor Coef SE Coef T-Value P-Value	
	Constant 62.95 16.4 3.85 0.001 Duration(min) 7.79 4.03 1.94 0.065	
	S=4.20970 R-sq=14.01% R-sq(adj)=10.27%	
	SD of residuals standard error of slope	
Calculating the Confidence Interval		
All of the components needed to calculate	e a confidence interval can be found on the AP Statistics	
formula sheet. Make sure you can locate th	ne information as you watch the video.	
Factors that Affect Interval Width		
Recall that confidence intervals in AP Statis	stics have the following structure:	
CI =	±	
The width of a confidence interval is	the	
For a confidence interval about the slope of a population,		
	=	
We generally prefer confidence	intervals (), so we want the margin of	
error to be There are two common ways to decrease margin of error.		
(1) the and	(2) the	
Calculating a Confidence Interval		
Raoul performed an experiment using 16 windup rubber band single-propellor airplanes. He wound		
up the propeller a different number of times and recorded the amount of time (in seconds) that the		
airplane flew for each number of rotations that the propellor was wound. A regression analysis was		
performed and the partial computer output is given below. Assuming that the conditions for		
inference are satisfied and calculate a 95%	C. Predictor Coef SE Coef T P	
	Constant 0.9241 0.6413 1.44 0.172	
	Rocacion 0.04025 0.01565 2.96 0.010	
	S = 0.5426 R-Sq = 38.4% R-Sq(adj) = 34.0%	



## Name Assuming that the conditions for inference are satisfied, which of the following is a 95 percent confidence interval for the slope of the regression line that relates to the number of rotations the rubber band is wound and plane's flight time? $CI = b \pm t^* \frac{s}{s_x \sqrt{n-1}} = b \pm t^* SE_b$ (A) $0.04625 \pm (2.145)(0.01565)$ (B) 0.9241 ± (2.145)(0.6413) (C) 0.04625 ± (2.131)(0.01565) (D) $0.04625 \pm (2.131) \left( \frac{0.5426}{\sqrt{16}} \right)$ (E) 0.9241 ± (2.131)(0.6413) What Should We Take Away? How do we determine the margin of error when estimating the slope of a population regression line? \_\_\_\_ = (critical value)(standard error of statistic) margin of error = \_\_\_\_\_= How do we calculate a confidence interval for the slope of a population regression line? Cl = \_\_\_\_\_± \_\_\_\_ $CI = b \pm t^* SE_b = b \pm t^* \frac{s}{s_x \sqrt{n-1}}$



# AP Statistics CED 9.3 Daily Video 1 (Skill 4.B)

What Will We Learn?		
How do we interpret a confidence interval for the slope of a population regression line?		
How do we justify a claim based on a confidence interval for slope?		
Old Faithful: 2019		
The scatterplot displays data on the duration (in minutes) and wait time until the next eruption (in		
minutes) for a random sample of 25 Old Faithful eruptions in July 2019, along with the sample		
regression line. Computer output from the least-squares regression		
analysis is shown below:		
Dradictor Coof CE Coof Theles D Value		
Constant $62.95$ $16.4$ $3.85$ $0.001$		
Duration(min) 7.79 4.03 1.94 0.065		
S=4.20970 R-sq=14.01% R-sq(adj)=10.27%		
Calculate and interpret a 95% confidence interval for the slope of		
the population regression line in 2019.		
Interpreting the Confidence Interval		
In general, here is how to interpret a confidence interval for the slope of a regression model:		
"We are confident that the from to the slope of the		
population regression line [].		
From Topic 9.2 Video 3, the 95% confidence interval is -0.55 to 16.13:		
"We are confident that the from to the slope of the		
until the next eruption (in		
minutes) from the of the previous eruption (in minutes) for Old Faithful		
geyser eruptions in July 2019."		
geyser eruptions in July 2019."		
geyser eruptions in July 2019." Interpreting Confidence Level In random sampling with the sample size, approximately C% of "C%"		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.         If we take random samples of size from the population of Old Faithful eruptions in		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.         If we take random samples of size from the population of Old Faithful eruptions in and use each sample to a 95% confidence interval for the		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.         If we take random samples of size from the population of Old Faithful eruptions in, and use each sample to a 95% confidence interval for the slope of the until the next		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.         If we take random samples of size from the population of Old Faithful eruptions in, and use each sample to a 95% confidence interval for the slope of the until the next eruption (in minutes) from the of the previous eruption (in minutes), about of		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.         If we take random samples of size from the population of Old Faithful eruptions in, and use each sample to a 95% confidence interval for the slope of the until the next eruption (in minutes) from the of the previous eruption (in minutes), about of the slope.		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.         If we take random samples of size from the population of Old Faithful eruptions in, and use each sample to a 95% confidence interval for the slope of the until the next eruption (in minutes) from the of the previous eruption (in minutes), about of those the slope.         Justifying a Claim		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.         If we take random samples of size from the population of Old Faithful eruptions in, and use each sample to a 95% confidence interval for the slope of the regression line for predicting until the next eruption (in minutes) from the of the previous eruption (in minutes), about of those would the slope.         Justifying a Claim         Does the confidence interval (-0.55 to 16.13) provide convincing evidence that wait time until the next		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.         If we take random samples of size from the population of Old Faithful eruptions in        , and use each sample to a 95% confidence interval for the         slope of the regression line for predicting until the next         eruption (in minutes) from the of the previous eruption (in minutes), about of         those would the slope.         Justifying a Claim         Does the confidence interval (-0.55 to 16.13) provide convincing evidence that wait time until the next         eruption of Old Faithful is linearly related to the duration of the previous eruption in July 2019?		
geyser eruptions in July 2019." Interpreting Confidence Level In random sampling with the sample size, approximately C% of "C%" confidence intervals created the slope of the regression line. If we take random samples of size from the population of Old Faithful eruptions in, and use each sample to a 95% confidence interval for the slope of the regression line for predicting until the next eruption (in minutes) from the of the previous eruption (in minutes), about of those the slope. Justifying a Claim Does the confidence interval (-0.55 to 16.13) provide convincing evidence that wait time until the next eruption of Old Faithful is linearly related to the duration of the previous eruption in July 2019? Note that $\beta = 0$ would indicate a line with a is the model for		
geyser eruptions in July 2019." Interpreting Confidence Level In random sampling with the sample size, approximately C% of "C%" confidence intervals created the slope of the regression line. If we take random samples of size from the population of Old Faithful eruptions in, and use each sample to a 95% confidence interval for the slope of the regression line for predicting until the next eruption (in minutes) from the of the previous eruption (in minutes), about of those would the slope. Justifying a Claim Does the confidence interval (-0.55 to 16.13) provide convincing evidence that wait time until the next eruption of Old Faithful is linearly related to the duration of the previous eruption in July 2019? Note that $\beta = 0$ would indicate a line with a is the model for wait time from eruption duration. In other words, the regression model would predict the		
geyser eruptions in July 2019." Interpreting Confidence Level Inrandom sampling with thesample size, approximately C% of "C%" confidence intervals createdthe slope of theregression line. If we takerandom samples of sizefrom the population of Old Faithful eruptions in , and use each sample toa 95% confidence interval for the slope of theregression line for predictinguntil the next eruption (in minutes) from theof the previous eruption (in minutes), aboutof thosewouldtheslope. Justifying a Claim Does the confidence interval (-0.55 to 16.13) provide convincing evidence that wait time until the next eruption of Old Faithful is linearly related to the duration of the previous eruption in July 2019? Note that $\beta = 0$ would indicate a line with a is the model for wait time from eruption duration. In other words, the regression model would predict the wait time until the next Old Faithful eruption no matter the duration of the previous eruption.		
geyser eruptions in July 2019." Interpreting Confidence Level In random sampling with the sample size, approximately C% of "C%" confidence intervals created the slope of the regression line. If we take random samples of size from the population of Old Faithful eruptions in, and use each sample to a 95% confidence interval for the slope of the regression line for predicting until the next eruption (in minutes) from the of the previous eruption (in minutes), about of those would the slope. Justifying a Claim Does the confidence interval (-0.55 to 16.13) provide convincing evidence that wait time until the next eruption of Old Faithful is linearly related to the duration of the previous eruption in July 2019? Note that $\beta = 0$ would indicate a line with a is the model for wait time from eruption duration. In other words, the regression model would predict the wait time until the next Old Faithful eruption no matter the duration of the previous eruption.		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.         If we take random samples of size from the population of Old Faithful eruptions in, and use each sample to a 95% confidence interval for the slope of the regression line for predicting until the next eruption (in minutes) from the of the previous eruption (in minutes), about of those would the slope.         Justifying a Claim         Does the confidence interval (-0.55 to 16.13) provide convincing evidence that wait time until the next eruption of Old Faithful is linearly related to the duration of the previous eruption in July 2019?         Note that $\beta = 0$ would indicate a line with a is the model for         wait time from eruption duration. In other words, the regression model would predict the         wait time until the next Old Faithful eruption no matter the duration of the previous eruption.         Because the confidence interval () contains as a		
geyser eruptions in July 2019." Interpreting Confidence Level Inrandom sampling with thesample size, approximately C% of "C%" confidence intervals createdthe slope of theregression line. If we takerandom samples of sizefrom the population of Old Faithful eruptions in, and use each sample toa 95% confidence interval for the slope of theregression line for predictinguntil the next eruption (in minutes) from theof the previous eruption (in minutes), aboutof thosewouldtheslope. Justifying a Claim Does the confidence interval (-0.55 to 16.13) provide convincing evidence that wait time until the next eruption of Old Faithful is linearly related to the duration of the previous eruption in July 2019? Note that $\beta = 0$ would indicate a line with a is the model for wait time from eruption duration. In other words, the regression model would predict the wait time until the next Old Faithful eruption no matter the duration of the previous eruption. Because the confidence interval () containsas a		
geyser eruptions in July 2019."         Interpreting Confidence Level         In random sampling with the sample size, approximately C% of "C%"         confidence intervals created the slope of the regression line.         If we take random samples of size from the population of Old Faithful eruptions in, and use each sample to a 95% confidence interval for the slope of the, and use each sample to a 95% confidence interval for the next eruption (in minutes) from the of the previous eruption (in minutes), about of those would the slope.         Justifying a Claim         Does the confidence interval (-0.55 to 16.13) provide convincing evidence that wait time until the next eruption of Old Faithful is linearly related to the duration of the previous eruption in July 2019?         Note that $\beta = 0$ would indicate a line with a is the model for wait time from eruption duration. In other words, the regression model would predict the wait time until the next Old Faithful eruption no matter the duration of the previous eruption.         Because the confidence interval () contains as a evidence that intil the next eruption of Old Faithful eruption.         Because the confidence interval (		



#### Interpreting a Confidence Interval

Raoul performed an experiment using 16 windup rubber band single-propellor airplanes. He wound up the propeller a different number of times and recorded the amount of time (in seconds) that the airplane flew for each number of rotations that the propellor was wound. A regression analysis was performed, and the conditions for inference were verified. A 95% confidence interval for the slope of the regression line that relates the number of rotations the rubber band is would and the plane's flight.		
time is given by (0.013, 0.080). Which of the following provides a correct interpretation of the		
confidence interval?		
<ul> <li>(A) There is a 0.95 probability that the slope of the population regression line that relates the number of rotations the rubber band is wound and the plane's flight time is between 0.013 and 0.080.</li> <li>(B) If the data collection process were repeated many times, about 95% of the resulting sample regression lines would have slopes between 0.013 and 0.080.</li> <li>(C) If the data collection process were repeated many times, about 95% of the resulting confidence intervals would contain the slope of the sample regression line.</li> </ul>		
(D) We are 95% confident that the slope of the sample regression line that relates the number of rotations		
the rubber band is wound and the plane's flight time is between 0.013 and 0.080.		
(E) We are 95% confident that the slope of the population regression line that relates the number of rotations		
the rubber band is wound and the plane's flight time is between 0.013 and 0.080.		
Justifying a Claim with a Cl		
(A) There is not convincing evidence of a linear relationship between the number of rotations of the rubber band		
(P) There is not convincing evidence of a linear relationship between the number of rotations of the rubber band		
and the flight times of windup airplanes like these because 0 is not included in the interval.		
(C) There is convincing evidence of a positive linear relationship between the number of rotations of the rubber		
band and the flight times of these 16 windup airplanes because all values in the interval are positive.		
(D) There is convincing evidence of a positive linear relationship between the number of rotations of the rubber		
band and the flight times of windup airplanes like these because all values in the interval are positive.		
(E) There is convincing evidence that there is not a linear relationship between the number of rotations of the		
rubber band and the flight times of windup airplanes like these because 0 is not included in the interval.		
What Should We Take Away?		
How do we interpret a confidence interval for the slope of a population regression line?		
"We are confident that the from to the slope of the		
population regression line [].		
How do we justify a claim based on a confidence interval for slope?		
If all the values in the confidence interval are with the claim, there		
convincing evidence for the claim.		
If one or more of the values in the confidence interval are		
there is convincing evidence for the claim.		



Distance

-2.158

S = 4.4336

## AP Statistics CED 9.3 Daily Video 2 (Skill 3.E)

#### What Will We Learn?

How do we construct and interpret a confidence interval for the slope of a population regression line?

#### 2019 International Exam #2

A real estate agent working in a large city believes that, for three-bedroom houses, the selling price of the house decreases by approximately \$2,000 for every mile increase in the distance of the house from the city center. To investigate the belief, the agent obtained a random sample of 20 three-bedroom houses that sold in the last year. The selling price, in thousands of dollars and the distance from the city center, in miles, for each of the 20 houses are shown in the scatterplot. The table shows computer output from a regression analysis of the data.

(a) Assume all conditions for inference are met. Construct and interpret a 95 percent confidence interval for the slope of the least-squares regression line.



0.149

0.000

-14.45R-sq = 92.1%

(b) Does the confidence interval contradict the agent's belief about the relationship between selling price and distance from the city center? Justify your answer.

#### 2019 International Exam #2(a) Calculate Interval

(a) Assume all conditions for inference are met. Construct and interpret a 95 percent confidence interval for the slope of the least-squares regression line.

We will construct a \_\_\_\_\_ confidence interval for  $\beta$  = \_\_\_\_\_ of the population regression line for \_\_\_\_\_ selling price (in thousands) from distance from the city center (in miles) for all three-bedroom houses near this city.

We will use a _ (Use the output ab	pove to create the <i>t</i> -interval.)	and fortunately conditions are	
<i>b</i> =	_ (Find on Output) df =	t* =	_ (use technology InvT)
Formula: CI =	$b \pm t^* SE_b$		
= .			
= .			
=			
<b>2019 International Exam #2, Part (a) Interpret Interval</b> Given: 95% CI = -2.471 to -1.845			
We are	that the slope of the _	regression line is between	and
thousands of _	This imp	lies that for additional mi	le that a three-
bedroom hous	e is away from the	_, the selling prince of the house is	s expected to
	between and	·	



#### 2019 International Exam #2

A real estate agent working in a large city believes that, for three-bedroom houses, the selling price of the house decreases by approximately \$2,000 for every mile increase in the distance of the house from the city center. To investigate the belief, the agent obtained a random sample of 20 three-bedroom houses that sold in the last year. The selling price, in thousands of dollars and the distance from the city center, in miles, for each of the 20 houses are shown in the scatterplot. The table shows computer output from a regression analysis of the data.

(b) Does the confidence interval contradict the agent's belief about the relationship between selling price and distance from the city center? Justify your answer.

Given: 95% CI = -2.471 to -1.845, Interpret the interval

Because the confidence interval contains \_\_\_\_\_, corresponding to a \_\_\_\_\_ decrease, it is a \_\_\_\_\_ value for the slope of the regression line. Consequently, the data \_\_\_\_\_

contradict the agent's belief that the selling prices of three-bedroom houses \_\_\_\_\_\_ about

\_\_\_\_\_ for every \_\_\_\_\_\_ increase in distance of the house from the city center.

#### What Should We Take Away?

How do we construct and interpret a confidence interval for the slope of a population regression line? **Make sure to:** 

- Define the \_\_\_\_\_ you are trying to estimate.
- Identify the \_\_\_\_\_ you are using.
- Verify that the \_\_\_\_\_\_ for the procedure are \_\_\_\_\_.
- \_\_\_\_\_\_ the confidence interval.
- \_\_\_\_\_ the interval in \_\_\_\_\_



## AP Statistics CED 9.4 Daily Video 1 (Skill 1.F)

Setting Up a Test for the Slope of a Regression Model



\_

Alternative Hypothesis		
In a statistical test, the h	ypothesis is the that we hope to support with	
from the data collected. In	the attendance and test scores example, the researchers	
wanted to know if there is a,	relationship between the	
of school days attended by Texas students	and the of questions answered correctly	
on the state Algebra 1 test. So the alternat	ive hypothesis is that the population regression line would	
have a In symbols:		
H <sub>0</sub> : $\beta$ >; where $\beta$ = of the	e population regression line for predicting number of	
questions answered correctly on the state t	test from the percent of school days attended for Texas	
Algebra 1 students.		
Stating Hypotheses: Summary		
For hypotheses about the of a po	pulation regression line:	
• The null is a statement of	, typically	
<ul> <li>The alternative always contains a st</li> </ul>	rict, typically	
When the inequality is	, the alternative is called	
When the inequality is	, the alternative is called	
The choice of alternative is determi	ned by the of interest and should be	
stated data collection	n begins.	
<ul> <li>Never refer to (such a</li> </ul>	ns b) in the hypotheses!	
<ul> <li>Remember to the</li> </ul>	·	
Don't Spill my Drink!		
Two AP Statistics students wondered if there	Speed         Spilled         Speed         Spilled           IS         (mph)         (mph)         (mph)         (mph)           100         100         100         100	
a linear relationship between speed and	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
amount of drink spilled when driving on bum	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
dirt roads. To find out, they filled a cup with	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
275 mL of water and placed it in the car's cu	O 20 65 50 95 20 60 50 75 40-	
holder, then drove down a bumpy road at a	20         50         50         105         30-           30         50	
specified speed and recorded how much wa	ter $\frac{30}{30}$ $\frac{75}{50}$ $\frac{20}{10}$ $\frac{15}{10}$ $\frac{10}{15}$ $\frac{10}{10}$ $\frac{15}{10}$ $\frac{10}{10}$	
spilled out. The 25 trials were randomly	30         75         10         15         20         25         50         30         30         50         © Daren Starnes	
assigned to be 5 trials each at 10, 20, 30, 40,	or 50 miles per hour (mph). Term Coef SE Coef	
Here are the data. (Note that several data po	sints have the same values for Speed (mph) 1.520 0.179	
speed and amount spilled.) A scatterplot of t	he data, along with computer S=12.6800 R-sq = 75.75%	
output from a least-squares regression analys	sis are shown. Do the data provide convincing evidence at	
the 0.05 significance level of a linear relation	ship between the car's speed on a bumpy dirt road and the	
amount of drink spilled? Assume the condition	ons for inference are met.	
Stating the Hypotheses		
H <sub>0</sub> : and H <sub>a</sub> :	; where	
What Should We Take Away?		
How do you state a null hypothesis in a test about the slope of a population regression line?		
$H_0: \beta = \beta_0$ For a null hypothesis of linear relationship,		
Note: remember to clearly define the $\beta$ .		
How do you state an alternative hypothesis in a test about the slope of a population regression line?		
$H_{\alpha}, \beta > \beta_0$ For a test of a positive linear relation	onship, For the test of a negative	
$\begin{array}{c} \begin{array}{c} & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & & \\ & & $	the test of a linear relationship,	



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## AP Statistics CED 9.4 Daily Video 2 (Skill 4.C)

Setting Up a Test for the Slope of a Regression Model

#### What Will We Learn?

How do we identify an appropriate significance test procedure for the slope of a population regression line?

How do we verify the conditions for performing a test about the slope of a population regression line?

#### Is Attendance the Solution?

Nationally, higher income areas tend to have fewer chronically absent students. Possible reasons:

- Transportation access
- Work to support family

#### Let's Look at the Data

Researchers collected data on the percent of school days attended and the number of questions answered correctly on the state's end-of-course test for a random sample of 11 Texas Algebra 1 students. Here are the data, along with a scatterplot and computer output from a least-squares regression analysis.

Percent attendance	95	89	67	98	99	76	92	91	76	85	82
Questions correct	45	42	31	51	49	38	46	41	35	39	37





attendance as the key to raising test scores for lower income students.

Poverty



Do the data give convincing evidence at the  $\alpha$  = 0.01 significance level of a positive, linear relationship between state test score and percent attendance for Texas Algebra 1 students?

#### Test Scores and Attendance - Hypotheses

In a previous video, we stated the hypotheses:  $H_0$ :  $\beta = 0$  and  $H_a$ :  $\beta > 0$ ; where  $\beta =$  the slope of the population regression line for predicting number of questions answered correctly on the state test from the percent of schools day attended for Texas Algebra 1 students.

#### Identifying the Procedure

You have learned many different significance test procedures this year. Some involved one sample and others involve two samples. Some involved inference about categorical data: \_\_\_\_\_\_ or

\_\_\_\_\_. Others involved inference about quantitative data: \_\_\_\_\_\_ or \_\_\_\_\_. When the goal is to test a claim about the \_\_\_\_\_\_ of a \_\_\_\_\_\_ regression line, we use a

## Checking Conditions

To perform a significance test about the slope of  $\beta$  of a population regression line, we must check the following:

- The true relationship between \_\_\_\_\_ is linear.
- The standard deviation of \_\_\_\_\_ doe not vary with \_\_\_\_/
- For a particular value of *x* the \_\_\_\_\_ (*y* values) are approximately normally distributed.
- There is independence in data collection: Data are collected using \_\_\_\_\_\_ sample of a randomized experiment. When sampling without replacement check that \_\_\_\_\_\_



Name
Checking Conditions (Be sure to ✓ your conditions!) <sup>32</sup>
To perform a significance test about the slope $\beta$ of a
population regression line, we must check the following:
• The true relationship between x and y is linear. $\begin{bmatrix} \frac{1}{2} & 4 \\ 4 & 2 \end{bmatrix}$
Scatterplot: The scatterplot show a, $\psi_{40}$
relationship between the percent
of school days attended by a student and the number of
correct answers on the state Algebra 1 test.
Residual Plot: The residual plots shows fairly © Daren Starres
scatter about line and no obvious curved pattern.
• The standard deviation of $y, \sigma_y$ does not vary with x.
<u>Scatterplot:</u> The number of correct answers vary by a
amount for the different percents of school days attended in the
data set.
R <u>esidual Plot:</u> The residuals are in size for the Percent of School Days Attended © Daren Stames
different percents of school days attended in the data set.
• For a particular value of $x$ , the responses ( $y$ – values) are approximately normally distributed.
Dotplot: A dotplot of residuals shows no obvious or
There is independence in data collection.
Data are collected using a random sample or a randomized experiment. The data come from a
sample of Texas Algebra 1 students.
When sampling without replacement, check that $n \leq 10\% N$ (all Texas Algebra 1 students)
All of the conditions are
What Should We Take Away?
How do we identify an appropriate significance test procedure for the slope of a population
regression line?
When testing a claim about the slope of a population regression line, use a
How do we verify the conditions for performing a test about the slope of a population regression
line?
* The true relationship between is linear. With and
* The standard deviation of $y, \sigma_y$ , does vary with $x$ . With and and
* For a particular value of x, the y-values are approximately normally distributed. With of
the or
* There is in data collection
Data are collected using a sample or a experiment.
When sampling replacement, check the



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## AP Statistics CED 9.5 Daily Video 1 (Skill 3.E)

Carrying Out a Test for the Slope of a Regression Model

#### What Will We Learn?

How do we calculate an appropriate test statistic in a test about the slope of a population regression line?

How do we calculate a p-value in a test about the slope of a population regression line?

#### Is Attendance the Solution?

Nationally, higher income areas tend to have fewer chronically absent students. Possible reasons:

Let's Look at the Data

Percent

attendance

Ouestions

correct

- Transportation access
  Work to support family
- Work to support family

Researchers collected data on the percent of school days

attended and the number of questions answered correctly on

the state's end-of-course test for a random sample of 11 Texas

Algebra 1 students. Here are the data, along with a scatterplot

and computer output from a least-squares regression analysis.

99 76 92 91 76 85 82

35 39 37





Poverty



Do the data give convincing evidence at the  $\alpha$  = 0.01 significance level of a positive, linear relationship between state test score and percent attendance for Texas Algebra 1 students?

46 41

#### Test Scores and Attendance – Hypotheses

95 89 67 98

42 31

45

51

49 38

In a previous video, we stated the hypotheses:  $H_0: \beta = 0$  and  $H_a: \beta > 0$ ; where  $\beta$  = the slope of the population regression line for predicting number of questions answered correctly on the state test from the percent of schools day attended for Texas Algebra 1 students. We will use  $\alpha = 0.01$ . We will use a *t*-test for slope and the conditions have all been met.

Calculating a Test Statistic	Predictor Coef SE Coef T P
In the attendance and test score study, $b = $	Constant -7.69 5.37 -1.43 0.186
This is evidence for $H_a$ : $\beta > \_$ because $b = \_$ >	Attendance 0.57 0.062 9.18 0.000 S = 1.99 R-Sg = 90.3% R-Sg (adi) = 89.3%
We want to know howit is to get evidence	3 - 1.99 N 34 - 90.8% N 34 (adj) - 69.8%
for H <sub>a</sub> this alone w	when $H_0$ is
After verifying the conditions are met, calculate the standardized te	est statistics:
standardized tests statistic = $\frac{\text{statistic} - \text{parameter}}{\text{standard error of the statistic}}$	$\frac{1}{tic}$ from formula sheet!!
Calculating a Test Statistic	Predictor Coef SE Coef T P
For a <i>t</i> -test for a slope, the standardized test statistic is: $t = \frac{b - \beta_0}{SE_b}$ ,	Constant -7.69 5.37 -1.43 0.186 Attendance 0.57 0.062 9.18 0.000
where $\beta_0$ is the value of $\beta$ specified by the null hypothesis. So, we	S = 1.99 K·Sq = 90.3% R-Sq (adj) = 89.3%
would have $t ==$	

\* All components can be found on the AP Statistics Formula Sheet! Make sure you can locate them!



Name	e				
Calculating the <i>p</i> -value					
Once we have calculated the standardized test statistic, use the _	with df =				
to calculate the . The p-value is the					
of values for the distribution	Constant -7.69 5.37 -1.43 0.186				
that are as than the observed	Attendance 0.57 0.062 9.18 0.000				
value of the test statistic	S = 1.99 R-Sq = 90.3% R-Sq (adj) = 89.3%				
Because our alternative hypothesis is $H: \beta > 0$ we want to find F	P(t > 1) in a t distribution				
with df –					
with dr =	for a one-tailed				
Vou can use Table R or Technology to find the pivalue –					
Den't Shill my Drinkl					
Don't Spill my Drink!	Numbers indicate repeated values in data set.				
I WO AP Statistics students wondered if there is (mph) (mL) (mph) (mL) 10 25 40 75 10 25 40 75	• 3 • 90 -				
	- Î Î 80- - Î Î 80-				
amount of drink spilled when driving on bumpy					
dirt roads. To find out, they filled a cup with $20  60  50  95$ 20  60  50  95 20  65  50  95	- 2 - 50- • • 3				
2/5 mL of water and placed it in the car's cup					
holder, then drove down a bumpy dirt road at a	$-\frac{30}{20}$ • 3				
specified speed and recorded how much water	- 10 15 20 25 30 35 40 45 50				
spilled out. The 25 trials were randomly	- Speed (mph) © Daren Starnes				
assigned to be 5 trials each at 10, 20, 30, 40, or 50 miles per hour (m	1ph). Term Coef SE Coef				
Here are the data. (Note that several data points have the same valu	es for Speed (mph) 1.520 0.179				
speed and amount spilled.) A scatterplot of the data, along with corr	1puter S=12.6800 R-sq = 75.75%				
output from a least-squares regression analysis are shown. Do the da	ata provide convincing evidence at				
the 0.05 significance level of a linear relationship between the car's s	peed on a bumpy dirt road and the				
amount of drink spilled? Assume the conditions for inference are me	t. Additionally, we have previously				
determined the hypotheses.					
Don't Spill My Drink!					
Calculate the standardized test statistic and <i>p</i> -value. From the pre	evious video we know that:				
$H_0$ :; where $\beta$ =;	line for predicting				
the amount of drink spilled (in mL) from the car's speed (in mph) o	on a bumpy dirt road. We will use				
$\alpha = $ because no significance level was stated. We will cond	uct a <i>t</i> -test for slope.				
As a reminder: $t = \frac{b - \beta_0}{b}$					
SEb					
Coloulating a gradue (Demonstration Table Demonstration)					
Calculating a p-value (Remember to use Table B or technology:)	P(t < 0.40) + P(t > 0.40) is a t				
Because our alternative hypothesis is $H_a$ : $\beta \neq 0$ , we want to find P	$(t \le -8.49) + P(t \ge 8.49)$ in a t				
distribution with df = =					
What Should We Take Away?					
How do we calculate an appropriate test statistic in a test about t	he slope of a population regression				
line? The Formula is $t = \frac{S - P_0}{SE_b}$ . But, often this information can be	found on the computer output!				
How do we calculate a <i>p</i> -value in a test about the slope of a popu	ulation regression line?				
If, p-value = $P(t \ge \text{observed test statistics})$ If, p-value	lue = $P(t \ge \text{observed test statistics})$				
If, p-value = $2 \times P(t \ge  \text{observed test statistics} )$ ; in a t dist	ribution with df.				



## AP Statistics CED 9.5 Daily Video 2 (Skill 4.B)

Carrying Out a Test for the Slope of a Regression Model

#### What Will We Learn?

How do we interpret the *p*-value in a test about the slope of a population regression line? How do we state a conclusion in a test about the slope of a population regression line?

#### Is Attendance the Solution?

Can education systems equalize opportunities for lower income students?

Nationally, higher income areas tend to have fewer chronically absent students. Possible reasons:

- Transportation access
- Work to support family







Some school systems have targeted attendance as the key to raising test scores for lower income students.

#### Let's Look at the Data

Researchers collected data on the percent of school days attended and the number of questions answered correctly on the state's end-of-course test for a random sample of 11 Texas Algebra 1 students. Here are the data, along with a scatterplot and computer output from a least-squares regression analysis.

Percent attendance	95	89	67	98	99	76	92	91	76	85	82	
Questions correct	45	42	31	51	49	38	46	41	35	39	37	



Do the data give convincing evidence at the  $\alpha$  = 0.01 significance level of a positive, linear relationship between state test score and percent attendance for Texas Algebra 1 students?

**Test Scores and Attendance - Hypotheses** In a previous video, we stated the hypotheses:  $H_0$ :  $\beta = 0$  and  $H_a$ :  $\beta > 0$ ; where  $\beta$  = the slope of the population regression line for predicting number of questions answered correctly on the state test from the percent of schools day attended for Texas Algebra 1 students. Use  $\alpha = 0.01$ . We will use a *t*-test for slope and the conditions have all been met.

Interpreting <i>p</i> -value	<b>e -</b> From previous vi	deos:		
<i>b</i> =, <i>t</i> = _	and <i>p</i> =v	/alue ≈		
<i>b</i> = is ev	idence	H_0: β=	_ and for $H_{a}$ : $\beta >$	_, because
The <i>p</i> -value measu	res how	it is to ge	t evidence for $H_a$ as	
than the observed o	evidence by	alo	one when $H_0$ is	Assuming there is
re	lationship between	state test so	ore and percent att	endance for Texas Algebra 1
students, there is a	n	probabi	lity of getting a sam	ple regression line with slope
or	by	alone in	a random sample o	f 11 Texas Algebra 1 students.
Making a Conclusion	on			
Small <i>p</i> -values ——	► test statistic	†	o occur by	chance alone.
Large <i>p</i> -values ——	▶ test statistic		to occur by	chance alone.
<ul> <li>Because the</li> </ul>	p-value of	_≤ <i>α</i> =	_, we reject H <sub>0</sub> .	
There is cor	ivincing	eviden	ce that [	].
Because the	p-value of	_≤α =	, we fail to reject <i>I</i>	-l <sub>0</sub> .
				_

There is not convincing \_\_\_\_\_\_ evidence that [



Making a Conclusion											
Do the data give convincing evidence at the $\alpha$ = 0.01 significance level of a positive, linear											
relationship between state test score and percent attendance for Texas Algebra 1 students?											
• $H_0: \beta$ vs. $H_a: \beta$ , where $\beta$ = the slope of the population regression line for											
predicting number of questions answered correctly on the state test from the percent of											
school days attended for Texas Algebra 1 students.											
Conditions are											
<ul> <li>b =, t = and p=value ≈</li> </ul>											
Because the <i>p</i> -value of <, we reject $H_0$ . There											
convincing statistical evidence of a between state test score and											
percent attendance for Texas Algebra 1 students.											
Don't Spill my Drink!											
Two AP Statistics students wondered if there is Two AP Statistics students wondered if there i											
a linear relationship between speed and $10 \frac{25}{10} \frac{40}{25} \frac{75}{40} \frac{90}{75}$											
amount of drink spilled when driving on bumpy $\begin{bmatrix} 10 & 23 & 40 & 75 \\ 10 & 15 & 40 & 55 \\ \hline 10 & 10 & 15 \\ \hline 10 & 10 & 15 \\ \hline 10 & 10 & 10 $											
dirt roads. To find out, they filled a cup with $20  60  50  95  70  95  70  95  70  95  70  95  70  95  70  95  70  95  70  95  95  70  95  95  95  95  95  95  95  9$											
275 mL of water and placed it in the car's cup $20  65  50  95$ 20  60  50  75											
holder, then drove down a bumpy road at a											
specified speed and recorded how much water											
spilled out. The 25 trials were randomly											
assigned to be 5 trials each at 10, 20, 30, 40, or 50 miles per hour (mph).											
Here are the data. (Note that several data points have the same values for Speed (mph) 1.520 0.179											
speed and amount spilled.) A scatterplot of the data, along with computer $S=12.6800$ R-sq = 75.75%											
output from a least-squares regression analysis are shown. Do the data provide convincing evidence at											
the 0.05 significance level of a linear relationship between the car's speed on a bumpy dirt road and the											
amount of drink spilled? Assume the conditions for inference are met.											
Interpreting the <i>p</i> -value											
From previous videos:											
• $H_0: \beta$ vs. $H_a: \beta$ , where $\beta$ = the slope of the regression line for predicting											
amount of spilled (in mL) from the car's speed (in mph) on a bumpy dirt road.											
<ul> <li>t-test for slope: Conditions are met.</li> </ul>											
• $b = $ , $t = $ and $p =$ value $\approx $											
Interpret the <i>p</i> -value.											
Assuming that there is relationship between the car's speed on a bumpy dirt road and											
the amount of drink spilled, there is a probability of getting a sample regression											
line with a slope as than in either direction by alone.											
Making a Conclusion											
Do the data provide convincing evidence at the 0.05 significance level of a linear relationship											
between the car's speed on a bumpy dirt road and the amount of drink spilled? From previous video:											
• $H_0: \beta$ vs. $H_a: \beta$ , where $\beta$ = the slope of the regression line for predicting											
amount of spilled (in mL) from the car's speed (in mph) on a bumpy dirt road.											
• Conditions are met. And $b$ =, $t$ = and $p$ =value $\approx$											
Because the <i>p</i> -value of, we There is convincing statistical											
evidence of a relationship between the car's speed on a bumpy dirt road and the											
amount of drink spilled.											



•

What Should We Take Away?	
How do we interpret the <i>p</i> -value in a te	est about the slope of a population regression line?
The <i>p</i> -value measures how	it is to get evidence for H₂ as or
than the observed evidence by chance	along with $H_0$ is
How do we state a conclusion in a test	about the slope of a population regression line?
• Because the <i>p</i> -value of	$\leq \alpha =$ , we reject $H_0$ .
There is convincing	evidence that [].
• Because the <i>p</i> -value of	$ \leq \alpha =$ , we fail to reject $H_0$ .
There is not convincing	evidence that [ ].



## AP Statistics CED 9.5 Daily Video 3 (Skill 4.B)

Carrying Out a Test for the Slope of a Regression Model

#### What Will We Learn?

How do we perform a complete significance test about the slope of a population regression line?

#### 2001 Exam #6 (Modified)

The Statistics Department at a large university is trying to determine if it is possible to predict whether an applicant will successfully complete the Ph.D. program or will leave before completing the program. The department is considering whether GPA (grade point average) in undergraduate statistics and mathematics courses (a measure of performance) and mean number of credit hours per semester (a measure of workload) would be helpful measures. To gather data, a random sample of 20 entering students from the past 5 years is taken. The data are given below:

Successfully Completed Ph.D. Program									Did Not Complete Ph.D. Program													
Student	A	В	С	D	E	F	G	Н	1	J	K	L	Μ		Student	Ν	0	Ρ	Q	R	S	Т
GPA	3.8	3.5	4.0	3.9	2.9	3.5	3.5	4.0	3.9	3.0	3.4	3.7	3.6		GPA	3.6	2.9	3.1	3.5	3.9	3.6	3.3
Credit hours	12.7	13.1	12.5	13.0	15.0	14.7	14.5	12.0	13.1	15.3	14.6	12.5	14.0		Credit hours	11.1	14.5	14.0	10.9	11.5	12.1	12.0

The regression output below resulted from fitting a line to the data in the group of 7 students that did not complete the Ph.D. program. The residual plot (not shown) indicated no unusual Predictor Coef StDev T P

patterns, and the assumptions necessary for inference were judged to be reasonable.

Did Not Complete Ph.D. Program											
Predictor	Coef	StDev	Т	Р							
Constant	24.200	3.474	6.97	0.001							
GPA	-3.485	1.013	-3.44	0.018							
S = 0.8408	R-Sq	= 70.3%									

(a) For the students who did not complete the Ph.D. program, is there a significant relationship between GPA and mean number of credit hours per semester at the  $\alpha = 0.01$  level?

$H_0: \beta = 0$ and $H_a: \beta \neq 0$ ; where $\beta$ = the slope of the regression line for predicting											
number of credit hours per semester from for students who did compl											
the statistics Ph.D. program at this large university. Use $\alpha = $ ; t-test for slope; Conditions are met!											
2001 Exam #6 (Modified)			I								
(a) For the students who did not complete the	e Ph.D. proc	aram, is the	ere a signifi	cant relatio	onship						
between GPA and mean number of credit bo	urs per	Did Not Comple	ete Ph.D. Program								
somester at the $\alpha = 0.01$ level?		Predictor	Coef 5	StDev 7	P 97 0.001						
semester at the $\alpha = 0.01$ level?		GPA S = 0.8408	-3.485 P. Sa = 70.30	1.013	44 0.018						
t =; dt =; p-value =		5 = 0.8408	K-Sq = 70.5%	0							
Because the <i>p</i> -value of	_, we		The	re is	_ convincing						
evidence of a relationship betw	veen GPA ar	nd mean n	umber of cr	edit hours	in the						
population of students at this university who	did not com	plete the s	statistics Ph	.D. progra	m.						
2001 Exam #6 (Modified)		1		1 0							
The regression output below resulted from fit	ting a line t	o the data	in the arou	p of 13 stu	udents that						
successfully completed the Ph D, program	Successfully Cor	upleted Ph.D. Pro	gram								
The second state (set she set) is disated as	Predictor	Coef	StDev	Т	Р						
The residual plot (not shown) indicated no	Constant	23.514	1.684	13.95	0.000						
unusual patterns, and the assumptions	unusual patterns, and the assumptions $\begin{bmatrix} GPA & -2.7555 & 0.4668 & -5.90 & 0.000 \\ S = 0.5658 & R-Sq = 76.0\% & -5.90 & 0.000 \end{bmatrix}$										
necessary for inference were judged to be											
reasonable.											
(b) For the students who successfully complet	ed the Ph.D	). program	, is the evid	ence for a	significant						

(linear) relationship between GPA and mean number of credit hours per semester stronger or weaker than for the students who did not complete the Ph.D. program? Justify your answer.



		Name				
001 Exam #6 (Modified) Successfully Completed Ph.D. Program						
Hint: You do not need to run a full test to	Predictor Constant GPA	Coef 23.514	StDev 1.684 0.4668	T 13.95	P 0.000 0.000	
answer this question. You only need to use	S = 0.5658	R-Sq =	= 76.0%	-5.90		
the computer output to the right.						
The <i>p</i> -value for a test of $H_0$ : $\beta$ =	0 and $H_a$ :	$\beta \neq 0$ ; whe	re $\beta$ = the _		_ of the	
population regression line for	nu	mber of cre	edit hours pe	er semeste	er	
GPA for students who successfully completed th	ne statistic	s Ph.D. prog	gram at this	large univ	versity, is	
. This p-value is	than	the '	p-valu	e for the t	est in part	
(a), and gives evidence of a		relation	iship betwee	en GPA ar	nd the	
mean number of credit hours per semester. You	could also	o compare <sup>·</sup>	the	fror	n the tests!	
What Should We Take Away?						
How do we perform a complete significance tes	t about th	e slope of a	population	rearessic	on line?	
Make sure to:						
State the and H	woothese	s and defin				
Give the	iypotnese.				•	
• Give the	'					
Identity the you are	using.					
Verify that the for th	e procedu	re are	•			
Calculate the and the		•				
• Make a based o	n the		(You do _	ne	eed to	
interpret the <i>p</i> -value unless specifically a	asked.)					



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# AP Statistics CED 9.6 Daily Video 1

Carrying Out a Test for the Slope of a Regression Model					
What Will We Learn?					
What inference methods did we learn about in Units 6 – 9?					
How can we identify the appropriate inference procedure to use in a given setting?					
Inference Recap					
Two main goals of inference:					
Estimating a parameter:					
Testing a claim:					
Appropriate inference method depends on type of data:					
Unit 6 Inference for Categorical Data:					
Unit 7 Inference for Quantitative Data:					
Unit 8 Inference for Categorical Data:					
Unit 9 Inference for Categorical Data:					
Confidence Intervals					
The formula on the formula sheet is the same for procedures.					
Cl =)()					
You should always do these steps:					
Define the you are trying to estimate.					
Identify the inference					
Verify the for the procedure are					
the confidence interval.					
• the interval					
You do need to interpret the confidence unless specifically asked.					
Significance Tests					
standardized test statistic = <u>statistic – parameter</u>					
standard error of the statistic					
You should always do these steps:					
State the and hypotheses. Be sure to parameter.					
Give the					
the inference procedure.					
Verify that the for the procedure are					
Calculate the and the					
Make a conclusion based on the					
You do need to interpret the unless specifically asked.					

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Unit 6				
	Ir	nference for Categorical Data: F	Pro	oportions
Goal	Method	Formula		Conditions
Estimate <i>p</i>	One-sample <i>z</i> interval for a proportion	$\hat{p} \pm z^* \sqrt{rac{\hat{p}(1-\hat{p})}{n}}$	•	Random sample/random assignment $n \le 10\% N$ (samp w/o replacement) $n\hat{p}$ and $n(1 - \hat{p}) \ge 10$
Test $H_0: p = p_0$	One-sample z test for a proportion	$z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1 - p_0)}{n}}}$	•	Random sample/random assignment $n \le 10\% N$ (samp w/o replacement) $np_0 \ge 10$ and $n(1 - p_0) \ge 10$
Estimate $p_1 - p_2$	Two-sample z interval for difference in proportions	$(\hat{p}_1 - \hat{p}_2) \pm z^* \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2}}$	•	Random samples/random assignment $n_1 \le 10\% N_1$ and $n_2 \le 10\% N_2$ (samp w/o replacement) $n_1\hat{p}_1, n_1(1-\hat{p}_1), n_2\hat{p}_2, n_2(1-\hat{p}_2) \ge 10$
Test $H_0: p_1 - p_2 = 0$	Two-sample z test for a difference in proportions	$z = \frac{(\hat{p}_1 - \hat{p}_2) - 0}{\sqrt{\frac{\hat{p}_C(1 - \hat{p}_C)}{n_1} + \frac{\hat{p}_C(1 - \hat{p}_C)}{n_2}}}$	•	Random samples/random assignment $n_1 \leq 10\%N_1$ and $n_2 \leq 10\%N_2$ (samp w/o replacement) $n_1\hat{p}_C, n_1(1-\hat{p}_C), n_2\hat{p}_C, n_2(1-\hat{p}_C) \geq 10$
Unit 7				
		Inference for Quantitative Dat	a:	Means
Goal	Method	Formula		Conditions
Estimate µ	One-sample t interval for a mean	$\bar{x} \pm t^* \frac{s}{\sqrt{n}}$	•	Random sample/random assignment $n \le 10\% N$ (samp w/o replacement) $n \ge 30$ or no strong skew/outliers
Test $H_0: \mu = \mu_0$	One-sample t test for a mean	$t = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$	•	Random sample/random assignment $\circ n \le 10\% N$ (samp w/o replacement) $n \ge 30$ or no strong skew/outliers
Estimate $\mu_1 - \mu_2$	Two-sample t interval for difference in means	$(\bar{x}_1 - \bar{x}_2) \pm t^* \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$	•	$\begin{array}{l} \mbox{Random samples/random assignment} \\ \circ \ n_1 \leq 10\% N_1 \mbox{ and } n_2 \leq 10\% N_2 \mbox{ (samp w/o replacement)} \\ n_1, n_2 \geq 30 \mbox{ or no strong skew/outliers} \end{array}$
Test $H_0: \mu_1 - \mu_2 = 0$	Two-sample t test for difference in means	$t = \frac{(\bar{x}_1 - \bar{x}_2) - 0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$	•	Random samples/random assignment $n_1 \le 10\% N_1$ and $n_2 \le 10\% N_2$ (samp w/o replacement) $n_1, n_2 \ge 30$ or no strong skew/outliers

### Unit 8

Inference for Categorical Data: Chi-Square						
Goal	Method	Formula	Conditions			
Test <i>H</i> <sub>0</sub> : Categorical variable has specified distribution	Chi-square test for goodness of fit	$\chi^2 = \sum \frac{(\text{observed} - \text{expected})^2}{\text{expected}}$	<ul> <li>Random sample/random assignment         <ul> <li>n ≤ 10%N (samp w/o replacement)</li> </ul> </li> <li>All expected counts &gt; 5.</li> </ul>			
Test <i>H</i> <sub>0</sub> : Categorical variable has same distribution for each population or treatment	Chi-square test for homogeneity	$\chi^2 = \sum \frac{\left(\text{observed} - \text{expected}\right)^2}{\text{expected}}$	<ul> <li>Random samples/random assignment         <ul> <li>n<sub>1</sub> ≤ 10%N<sub>1</sub>, n<sub>2</sub> ≤ 10%N<sub>2</sub>, (samp w/o replacement)</li> </ul> </li> <li>All expected counts &gt; 5.</li> </ul>			
Test <i>H</i> <sub>0</sub> : There is no association between two categorical variables in a population	Chi-square test for independence	$\chi^2 = \sum \frac{(\text{observed} - \text{expected})^2}{\text{expected}}$	<ul> <li>Random sample/random assignment         <ul> <li>n ≤ 10%N (samp w/o replacement)</li> </ul> </li> <li>All expected counts &gt; 5.</li> </ul>			



Inference for Quantitative Data: Slopes							
Goal Metho	d Formula	Formula			Conditions		
Estimate <i>t</i> interval β a slope	$b \pm t^* SE_b = b \pm t^* - \frac{1}{s_b}$	$b \pm t^*SE_b = b \pm t^* \frac{s}{s_x \sqrt{n-1}}$ • The true • The state • For a para proxi • There is • Rand • n \leq		The relationship between $x$ and $y$ is linear. andard deviation of $y$ doesn't vary with $x$ . articular value of $x$ , the $y$ -values are imately normally distributed. s independence in data collection. dom sample or randomized experiment. 10%N (samp w/o replacement)			
Test $H_0: \beta = \beta_0$ a slope	$t = \frac{b - \beta_0}{SE_b}$	$t = \frac{b - \beta_0}{SE_b}$ • The true • The state • For a para proximation of the state of the st			the relationship between $x$ and $y$ is linear. And and deviation of $y$ doesn't vary with $x$ . And ard deviation of $x$ , the $y$ -values are articular value of $x$ , the $y$ -values are artimately normally distributed. Is independence in data collection. Adom sample or randomized experiment. If $10\%N$ (samp w/o replacement)		
Selecting an Inferer	ce Procedure						
	In	ference for					
Categorical Data: Proportions	Quantitative Data: Means	Categorical Dat	ta: Chi-So	quare	Quantitative Data: Slopes		
One-sample <i>z</i> interva for a proportion	One-sample <i>t</i> interval for a mean (Paired data)	Chi-square test fo (Distribution of ) one categorid	Chi-square test for goodness of fit (Distribution of proportions for one categorical variable)			<i>t</i> interval for a slope	
One-sample <i>z</i> test for a proportion	One-sample <i>t</i> test for a mean (Paired data)	Chi-square test for homogeneity (Distribution of a categorical variable for multiple populations or treatments)			<i>t</i> test for	a slope	
Two-sample <i>z</i> interva for a difference in proportions	Two-sample <i>t</i> interval for a difference in means	Chi-square test fo (Relationship categorical	Chi-square test for independence (Relationship between two categorical variables)				
Two-sample <i>z</i> test for a difference in proportions	Two-sample <i>t</i> test for a difference in means						
<b>1997 Exam #5</b> A company bakes computer chips in two ovens, oven A and oven B. The chips are randomly assigned to an oven and hundreds of chips are baked each hour. The percentage of defective chips coming from these ovens for each hour of production throughout a day is shown below.							
The percentage of defective chips produced each hour by oven A has a mean of 33.56 and a standard deviation of 5.20. The				Oven A	Oven B		
percentage of defective chips produced each hour by oven B has a mean of 32.44 and a standard deviation of 3.78. The hourly differences in percentages for oven A minus oven B have a mean of 1.11 and a standard deviation of 4.28.			1 2 3 4 5	45 32 34 31 35 37	36 37 33 34 33 32		
Does there appear to be a difference between oven A and oven B with respect to the mean percentages of defective chips produced? Give appropriate statistical evidence to support your answer.			7 8 9	31 30 27	33 30 24		
Individual/case: Inference for:							
Variable(s) of interest: One sample, Paired data, or Two Samples					Samples?		
Type of data:       Estimate parameter or Test a Claim?    Perform:							



Name\_\_\_\_\_

Name Larry Green's Applet Source: Larry Green's Comprehensive Review applet, http://www.ltcconline.net/greenl/java/Statistics/catStatProb/categorizing StatProblemsJavaScript.html Is political affiliation related to the month that the person was born in? 3000 voters were studied. Individual/case: \_\_\_\_\_\_ Variable(s) of interest: \_\_\_\_\_\_ Type of Data: \_\_\_\_\_ Inference for: \_\_\_\_\_ 1 Variable, 2 Variables (one sample) or 2 Variables (multiple samples or treatments)? Inference Procedure: \_\_\_\_\_ • Confidence Interval for a Population Mean • Confidence Interval for a Proportion o Confidence Interval for the Diff. Between 2 Means (Independent Samples) • Confidence Interval for Paired Data (Dependent Samples) • Confidence Interval for the Difference Between 2 Proportions • Prediction for a Single Value of y for a Fixed x • Hypothesis Test for a Population Mean • Hypothesis Test for a Population Proportion • Hyp. Test for the Difference Between 2 Means (Independent Samples) • Hyp. Test for Paired Data (Dependent Samples) • Hyp. Test for the Difference Between 2 Proportions Chi-Square Goodness of Fit Test • Chi-Square Test for Independence • Chi-Square Test for Homogeneity Is political affiliation related to the month that the person was born in? 3000 voters were studied. 

 Individual/case:
 Variable(s) of interest:

 Type of Data:
 Inference for:

 1 Variable, 2 Variables (one sample) or 2 Variables (multiple samples or treatments)? Inference Procedure: \_\_\_\_\_ What Should We Take Away? What inference methods did we learn about in Units 6 – 9? Unit 6 Inference for Categorical Data: Unit 7 Inference for Quantitative Data: \_\_\_\_\_ Unit 8 Inference for Categorical Data: \_\_\_\_\_ Unit 9 Inference for Categorical Data: \_\_\_\_\_ How can we identify the appropriate inference procedure to use in a given setting? Individual/case: Variables of interest: Type of Data: Inference for:

